Class 10th

Mathematics

<u>Circles</u>

Circle:

A circular path equidistant from a fixed point (Centre) is called circle.

Diameter:

A diameter is a line segment from one point to another point on circumference which passes through the centre of the circle. In the given circle PQ is diameter



Radius:

Radius is a line segment from centre to any point of the boundary of the circle. Radius is half of the diameter. In the given circle, OR is the radius.

Circumference:

The length of the boundary of the circle is called circumference of circle. It is calculated by using the formula $2\pi r$ or πd , where 'r' is the radius and 'd' the diameter of circle.

Chord:

A chord in a circle is a line segment which has the end points on the boundary of the circle. In the given circle, both AB and PQ are the chords. PQ is also the diameter and the chord.

Tangent:

A tangent is a line segment which touches the circle only at one point. In the given figure, AE is a tangent which touches the circle at point P



Secant:

A secant is a line segment which touches the circle at two different points. In the given circle, AB is a secant which the touches the circle at point O and B



Pair of tangents:

From an external point, two tangents are drawn to a circle. In this figure, from external point P, two tangents PR and PQ are drawn. These tangents touch the circle at R and Q respectively. Also, PR = PQ.



At any point on the circumference of the circle, we can draw only one tangent. In this way we can as many as tangents to a circle.

Concentric Circles with same centre:

Two or more circles are said to be concentric with common centre if they have common centre and of different radii. (See given figure) In this figure, there are two concentric circles with same centre O and having radii as OQ and OP



Concentric Circles with different centres:

Two or more circles are said to be concentric with different centres if they lie in one another and their centres are different. (See given figure) In this figure, there are two concentric circles centre O and P. The bigger circle has the centre O and the smaller circle P



Questions for Practice

Objective type

- Q.No.1. A line segment which touches the circle at two different points and passes out from the circle is called:
 - a) Chord b) Secant
 - c) Tangent d) Radius
- Q.No.2. A line segment which touches the circle only at one point is called:
 - a) Chord b) Secant
 - c) Tangent d) Diameter
- Q.No.3. How many tangents can be drawn from an external point to a circle?

a) 1	b) 2
c) Infinite	c) 0

- Q.No.4. How many tangents can be drawn from a point on the boundary of a circle?
 - a) only 1 b) Infinitely many
 - c) More than one d) 0
- Q.No.5. ABCD is a cyclic quadrilateral with $\angle A = 80^{\circ}$ and $\angle B = 90^{\circ}$. The measure of $\angle C$ and $\angle D$ is respectively;
 - a) $90^{\circ}, 90^{\circ}$ b) $100^{\circ}, 80^{\circ}$
 - c) $100^{0}, 90^{0}$ d) $90^{0}, 100^{0}$

Q.No.6.	If two circles touch each other at one point only, the nu common tangents to the circles are;		
	a) 2	b) 1	
	c) Infinite	d) None	
Q.No.7.	A circle can have parallel tangles.		
	a) 2	b) 4	
	c) 0	d) Infinite	
Q.No.8. Two circles which do not touch each other tangents in common.		each other will have	
	a) 0	b)1	
	c) 4	d) Infinite	
Q.No.9.	A tangent touches the circle at points		
	a) 1	b) 2	
	c) Infinite points	d) 4	
Q.No.10.	How many tangents can be drawn from a point which is inside the circle?		
	a) Infinite	b) Only one	
	c) No tangent	d) More than one	

In the given figure, C1 and C2 are concentric Q.No.11. circles with common centre O. If PQ the chord of circle C1 is tangent to circle C2, which one of the following may not be true?

- a) OP = OR
- b) PQ = QR
- c) OR = QR

c) 360⁰

Q.No.12.

d) $\triangle OPQ$ is right angled triangle



In the given circle, <i>F</i>	^{P}Q is a tangent and OD the		
radius. The measure	e of \angle PDO is equal to	(^o)
a) 180 ⁰	b) 90 ⁰		
c) 360 ⁰	d) 100 ⁰	P	D Q

- Q.No.13. Tangent and the radius which meets the circle at the contact point of tangent are to each other.
 - a) Perpendicular b) parallel
 - c) Coincident d) All of these
- Q.No.14. Two tangents to a circle are parallel to each other. The line segment joining the point of contacts of the tangents is as
 - a) radius b) Diameter
 - c) Any chord d) Secant
- Q.No.15. The longest chord in the circle is
- Q.No.16. A chord which passed through the centre of the circle is called
- Q.No.17. The line joining the point of contacts of two parallel tangents of a circle must pass through
- We can have only three concentric circles (true/False) Q.No.18.

Very Short Answer Type Questions

- Q.No.1 Draw a rough sketch of a circle and a pair of tangents to it from any external point.
- Q.No.2. Draw a circle with centre *P*. Draw any two tangents which are parallel to each other.
- Q.No.3. In the given figure, *PQ and RS* are two tangents parallel to each other. Show that *AB* is diameter



- Q.No.4. Draw a rough sketch of any four parallel pairs of tangents.
- Q.No.5. In the given figure, AQ is a tangent and AB the diameter of the circle with centre O. Show that ABQ is a right-angled triangle.



Q.No.6. In the given figure, PQ = RQ. If diameter PQ = 12cm, Find PR.



- Q.No.7. Draw two concentric circles with common centre. Draw a line segment which is tangent to one circle and chord to another circle.
- Q.No.8. Draw three concentric circles. Draw a line segment which chord in one circle, secant in another circle and tangent in third circle.
- Q.No.9. Is it possible to have two circles with two points in common? If yes, draw at least one.

Short Answer Type Questions

- Q.No.1. *AB* and *AC* are two tangents which meets the circle at *B* and *C* respectively. If OA = 17cm and AB = 15cm, find the radius of the circle.
- Q.No.2. In the given figure, PQ is the tangent to the circle with centre O. If OP = PQ, show that $OQ = \sqrt{2}OP$



Q.No.3. In the given figure, AC and BC touches the circle at two points A and B respectively. If $\angle ABC = 60$ and $\angle AOB = 120$, prove that AC and BC are two tangents.



Q.No.4. Draw a circle with centre P. Draw two tangents to it from the external point D which meet the circle at points B and C. If the radius of the circle is 7cm and the distance between the external point D to the centre of the circle is 10cm, find the length of each tangent

- Q.No.5. A tangent from *P* is 16*cm* to the circle with radius 12*cm*. Find the distance between the centre of the circle and the point *P*.
- Q.No.6. In the given figure, PS, SR, RQ and QP are the tangents to the circle. If PQRS is a parallelogram and AP = BQ = SD, prove that PQRS is a rhombus.

Q.No.7. In the given figure, AB is the tangent to the circle with centre O. If BP = AP, show that BO = OA

- Q.No.8. In the given figure, AB and DC are two tangents which meets the opposite ends of the diameter PR. If PB = RC, prove that PBCR is a rectangle.
- Q.No.9. Prove that the tangents drawn from external point to the circle are equal.



Q



Long Answer Type Questions





Q.No.2. AB, BC, CD and DA are the tangents to the circle which touches the circle at P, Q, R and S respectively. If PB =9.6cm, DC = 12cm and AS = 3.7cm, find the perimeter of quadrilateral ABCD



Q.No.3. In the given figure, AC = 15cmis a tangent to circle which meets the circle at C. If AB = 10cm, find the radius of circle.



Q.No.4. In the given figure, PQ and PQare two tangents to the circle with centre O. If $\angle QPR = 40$, find;

a) $\angle ROQ$ b) $\angle ORP$

c) $\angle OQR$ d) $\angle RSQ$



Q.No.5. BC and AC are two tangents which touches the circle at B and D respectively. If AX =6, AD = 12cm and BC = 18, find the radius of the circle.



z

Α

х

в

Q.No.6. A tangent AB touches the circle at Y. If XY is a chord such that $\angle XYB = 65^{\circ}$. Find $\angle XOY$

Q.No.7. In the given circle of radius 6*cm*, Chord *AB* is equal to its radius. Tangent *BC* is equal to the chord *AB*. Find the length of *OC*



Y

Q.No.8. AD and DC are two tangents from external point D which meets the circle at point A and C respectively. If $\angle ABC =$ 70, $\angle AEC = 110$, find $\angle ADC$ and Obtuse $\angle AOC$.



Q.No.9. In the given figure, *BR* and *BS* are two tangents which meets the circle at points *R* and *S* respectively. If $\angle PBA = 40$, PO = AO and *PA* the tangent which meets the circle at point *T*, find $\angle POA$



Q.No.10. In the given figure, AB and OD are the radii of circle with centre O and PB & PC are the radii of circle with centre P. If AO = 7cm, PB = 3.5cm and AB = 12cm, find the area of polygon AODCPB



Q.No.11. In the given figure, AC and BC are two tangents from the point C. Also, AD and BD are two tangents from the point D. If the radius of the circle is $6 \ cm, BD = 8 \ cm$ and $DC = 5 \ cm$, find the length of OC and BC



In the given figure, AB, BC, CD, DA are Q.No.12. Α Ρ в the tangents to the circle. If AB || SQ || DC and AD || PR || BC, show that *ABCD* is a square. q s D R In the given figure, AB is a Q.No.13. tangent to the circle. If $\angle ABD = 30$, find $\angle DCA$. 30 Also show that $\angle ABO =$ 90 – 2∠*ACD* Answers Q1, b Q2, c Q3, b Q4, a Q5, c Q6, b Q7, d Q8, a Q9,a Q10, c Q11, c Q12, b Q13, a Q14, b Q15, Diameter Q16, Diameter Q17, Centre Q18, False Very Short Answer Type $12\sqrt{2}$ cm Q6 Q9, Yes Short Answer Type Q5, $\sqrt{51}$ Q1, 8cm Q5, 20cm Long Answer type Q3, $\frac{25}{4}$ cm Q1, 60cm Q2, 50.6cm Q4, ∠ROQ =140, ∠ORP =90, ∠OQR=20, ∠RSQ=70 Q5, 9cm Q6, 130, Q7, 10cm Q8, ∠ADC=40, ∠AOC=140 Q9, 170 Q10, 136 cm², Q11, 0C= 15cm, BC = $\sqrt{189}$