

INDIAN ASSOCIATION OF PHYSICS TEACHERS

National Standard Examination in Astronomy - 2023

Date of Examination: November 25, 2023 Time: 2:30 PM to 4:30 PM

Question Paper Code: 41

Student's					
Roll No:					

Write the Question Paper code (mentioned above) on YOUR OMR Answer Sheet (in the space provided), otherwise your Answer Sheet will NOT be evaluated. Note that the same Question Paper Code appears on each page of the Question Paper.

Instructions to Candidates:

- 1. Use of mobile phone, smart watch, and iPad during examination is STRICTLY **PROHIBITED.**
- 2. In addition to this Question Paper, you are given OMR Answer Sheet along with candidate's copy.
- 3. On the Answer Sheet, make all the entries carefully in the space provided **ONLY** in **BLOCK CAPITALS** as well as by properly darkening the appropriate bubbles.

 Incomplete/ incorrect/ carelessly filled information may disqualify your candidature.
- 4. On the OMR Answer Sheet, use only **BLUE or BLACK BALL POINT PEN** for making entries and filling the bubbles.
- 5. Your **Ten-digit roll number and date of birth** entered on the OMR Answer Sheet shall remain your login credentials (means login id and password respectively) for accessing your performance / result in National Standard Examination in Astronomy 2023.
- 6. Question paper has two parts. In part A1 (Q. No.1 to 48) each question has four alternatives, out of which **only one** is correct. Choose the correct alternative and fill the appropriate bubble, as shown.

Q.No.22 a c d

In part A2 (Q. No. 49 to 60) each question has four alternatives out of which any number of alternative (s) (1, 2, 3, or 4) may be correct. You have to choose **all** correct alternative(s) and fill the appropriate bubble(s), as shown

Q.No.54 a c

- 7. For **Part A1**, each correct answer carries 3 marks whereas 1 mark will be deducted for each wrong answer. In **Part A2**, you get 6 marks if all the correct alternatives are marked. No negative marks in this part.
- 8. Rough work may be done in the space provided. There are 11 printed pages in this paper
- 9. Use of **Non programmable scientific** calculator is allowed.
- 10. No candidate should leave the examination hall before the completion of the examination.
- 11. After submitting Answer Paper, take away the Question Paper & candidate's copy of OMR sheet for your future reference.

Please DO NOT make any mark other than filling the appropriate bubbles properly in the space provided on the OMR Answer Sheet.

Answer Sheets are evaluated using machine, hence CHANGE OF ENTRY IS NOT ALLOWED. Scratching or overwriting may result in wrong score.

DO NOT WRITE ON THE BACK SIDE OF THE ANSWER SHEET.

Instructions to Candidates (Continued):

You may read the following instructions after submitting the Answer Sheet.

- 12. Comments/Inquiries/Grievances regarding this Question Paper, if any, can be shared on the Inquiry/Grievance column on www.iapt.org.in on the specified format till December 3, 2023
- 13. The answers/solutions to this Question Paper will be available on the website: www.iapt.org.in by December 2, 2023. The score card may be downloaded after Dec 24, 2023

14. CERTIFICATES and AWARDS:

Following certificates shall be awarded by IAPT to the students, successful in the NATIONAL STANDARD EXAMINATION IN ASTRONOMY -2023

- (i) "CENTRE TOP 10 %" To be downloaded from iapt.org.in after 30.01.24
- (ii) "STATE TOP 1 %" Will be dispatched to the examinee
- (iii) "NATIONAL TOP 1 %" Will be dispatched to the examinee
- (iv) "GOLD MEDAL & MERIT CERTIFICATE" to all students who attend OCSC 2024 at HBCSE Mumbai

Certificate for centre toppers shall be uploaded on iapt.org.in

- 15. List of students (with centre number and roll number only) having score above **Minimum Admissible Score** (**MAS**) will be displayed on the website: **www.iapt.org.in** by **December 25, 2023. See the MAS clause** on the Student's brochure on the web.
- 16. List of students eligible to appear for Indian National Astronomy Olympiad (INAO 2024) shall be displayed on **www.iapt.org.in** by December 30, 2023.

Physical constants you may need....

Magnitude of charge on electron $e = 1.60 \times 10^{-19} C$	Faraday constant = 96,500 <i>C</i> / <i>mol</i>
Mass of electron $m_e = 9.11 \times 10^{-31} kg$	Speed of light in free space $c = 3 \times 10^8 \text{ ms}^{-1}$
Mass of proton $m_p = 1.67 \times 10^{-27} kg$	Speed of sound in dry air at 0°C $v = 332 \text{ ms}^{-1}$
Mass of neutron $m_n = 1.67 \times 10^{-27} kg$	Permittivity of free space $\varepsilon_0 = 8.85 \times 10^{-12} C^2 / Nm^2$
Acceleration due to gravity $g = 9.81 \text{ ms}^{-2}$	Permeability of free space $\mu_0 = 4\pi \times 10^{-7} \ H \ / \ m$
Universal gravitational constant $G = 6.67 \times 10^{-11} Nm^2 / kg^2$	Planck's constant $h = 6.626 \times 10^{-34} Js$
Universal gas constant $R = 8.31 \ J / mol \ K$	Rydberg constant $R = 1.097 \times 10^7 m^{-1}$
Boltzmann constant $k = 1.38 \times 10^{-23} J / K$	Astronomical unit = $1.50 \times 10^{11} m$
Stefan's constant $\sigma = 5.67 \times 10^{-8} W / m^2 K^4$	Radius of Sun $R = 6.96 \times 10^8 m$
Avogadro's constant $A = 6.022 \times 10^{23} mol^{-1}$	Mass of Sun $M = 2.0 \times 10^{30} kg$

INDIAN ASSOCIATION OF PHYSICS TEACHERS NATIONAL STANDARD EXAMINATION IN ASTRONOMY

(NSEA - 2023)

	Time: 120 minute Atter	mpt All Sixty Questions	Max. Marks: 216			
		A – 1 ONS IS CORRECT. BUBBLE THE	CORRECT OPTION.			
1.	Venus has an equatorial radius of 605 0.72 AU. The smallest diameter of the used to just resolve the Venus disc during (a) 200 cm (b) 20 cm	primary mirror/lens (objective) o ng the transit of Venus is approxi	f an optical telescope to be			
2.	The Earth's atmosphere is transparent at the electromagnetic spectrum. Choose to (a) ultraviolet (c) some portions of the radio way.	the correct option to fill the blank (b) X-ray				
3.	It is given that the pupil of the human light-gathering power does a telescope have than the human eye?					
	(a) 4 times (b) 16 tim	nes (c) 40 times	(d) 1600 times			
4.	An astronomer observes a spectral emissame spectral line is measured in the wavelength 500 nm. The speed of the glight c) is equal to (a) 0.2 c moving away from Earth (c) 0.9 c moving away from Earth	laboratory using a stationary so galaxy toward or away from Eart (b) 0.2 c moving to	ource and is seen to have th (in units of the speed of oward Earth			
5.	An astronomer observes that Polaris is about the longitude of her location from (a) nothing (c) that it is 50 degrees south		grees north			
6.	The spectrum of a cloud of cool gas seen against a bright background black body would show (a) bright lines (emission spectrum) against a continuum spectral emission background (b) a continuous spectrum (c) dark lines (absorption lines) against a continuum emission background (d) either bright or dark lines, depending on distance, against a continuum emission background					
7.	If a star has a parallax of one-eighth of (a) 2,06,265 astronomical units (c) one-eighth parsec	a second of arc, its distance from (b) eight light year (d) eight parsec				
8.	The elemental composition of the Sun, (a) 50 % metals, 50 % hydrogen (b) 71 % hydrogen, 27 % helium, 2 (c) 75 % helium, 20 % hydrogen, 5 (d) 75 % carbon, 25 % helium	2 % others				
9.	Which of the following planets has esse	entially no atmosphere?				

(c) Jupiter

(b) Mercury

(d) Mars

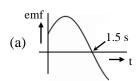
(a) Venus

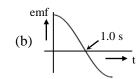
- 10. Sunspots are
 - (a) relatively cool compared to the photosphere
 - (b) related to convection cells
 - (c) related to the Sun's electric field
 - (d) cyclonic storms similar to Jupiter's great red spot
- 11. A planet moves fastest in its orbit
 - (a) when it is in opposition

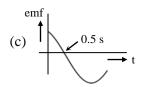
(b) when it is closest to the Sun

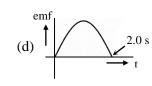
(c) the greater its mass

- (d) when it is farthest from the Sun
- 12. A square loop of side 10 cm and resistance 0.5Ω is placed vertically in the east-west (x-z) plane. A uniform magnetic field of strength B = 0.1T is set up across the plane of the coil in the north-south direction. The coil is rotating about a vertical axis $(\vec{\omega} || \hat{k})$ through its center at the rate of one rotation per 4 second. At time t = 0, the plane of the coil makes an angle $\theta = +45^{\circ}$ with the east-west (x-z) plane. The correct schematic diagram giving the emf induced in the coil is



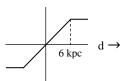




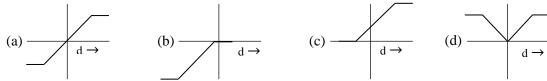


- 13. In 1912 Henrietta Leavitt making observations of Cepheid variable stars in the Magellanic clouds discovered the *period luminosity relation* fainter stars have shorter periods. The relation between the apparent magnitude m (the measured magnitude of a star situated at its actual distance D pc) and its absolute magnitude M (its magnitude if located at a distance of 10 pc) is given by the magnitude distance relation m M = 5 log D 5. Here D is the distance in parsec. The distance from Milky Way to the Andromeda galaxy is 765 kpc. The observed period luminosity relation determined by observations in the K band for Cepheid variables in the Andromeda galaxy is $m_K = -3.26 \ (log\ P-1) + 18.73$ with slope 3.26 and zero-point 18.73. For Cepheids in the Milky Way $M_K = -3.26 \ (log\ P-1) + c$ where c is approximately
 - (a) 5.69
- (b) 5.67
- (c) +18.73
- (d) 10.67
- 14. A Red Giant star of mass $M_{Red\ Giant}$ and a White Dwarf star of mass $m_{White\ Dwarf}$ form a binary system and are rotating in circular orbits around their common centre of mass with a period of one year. The White Dwarf is orbiting just within the photosphere of the Red Giant star. The Red Giant has a radius of 3.6 AU. An estimate for the mass of the Red Giant star in solar mass units is (note that $m_{White\ Dwarf} \ll M_{Red\ Giant}$)
 - (a) 188
- (b) 94
- (c) 47
- (d) 13
- 15. In spectroscopy doublet lines are closely spaced spectral lines that arise from transitions from a common fundamental state to states which differ only in their total angular momentum value. If a source of light is moving away from us the light from the source will appear shifted to the longer wavelength (red) side of the spectrum. The shift is quantified by the redshift $z = \frac{\Delta \lambda}{\lambda} = \frac{v}{c}$, where λ is the observed wavelength of the spectral line when the emitting source is at rest with respect to the observer and $\Delta\lambda$ is the observed shift in the wavelength. Hubble observed that spectral lines of galaxies not very close to us are redshifted. A galaxy is showing a redshift of z = 0.005. The observed wavelength separation, in nanometre, of the sodium doublet at 589 and 589.6 nm and of the potassium doublet at 766.5 and 769.9 nm in the spectrum of the galaxy are respectively
 - (a) 0.603, 3.417
- (b) 0.003, 0.017
- (c) 38.33, 29.45
- (d) 38.33, 38.5

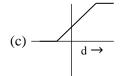
16. The rotation curve of a spiral galaxy gives the 'instantaneous' local mean tangential velocity in the plane of the galaxy of stars/gas clouds in the galaxy lying along a line through the centre of the galaxy, with respect to the distant quasars as observed from the centre of the galaxy. The following is a schematic diagram of the rotation curve of a particular spiral galaxy.

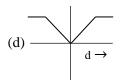


As measured from a star orbiting at a distance r = 8 kilo parsec from the centre, which one of the following diagrams gives a schematic representation of the mean tangential velocity v(d) with which objects at various distances d from the star, along the line joining the star to the centre of the galaxy, will appear to move with respect to the distant quasars?









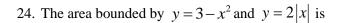
- 17. The relation R on Z the set of integers, defined by $(x, y) \in R$ if and only if $xy \neq 0$ is
 - (a) Reflexive, symmetric and transitive
- (b) Reflexive, symmetric but not transitive
- (c) Symmetric, transitive but not reflexive
- (d) Transitive, reflexive but not symmetric
- 18. A is a 3×3 non-singular matrix such that $A^4=4A$. What is the determinant of A? (c) 16
- 19. The number of real values of θ that satisfy the equation $\sin^2 \theta 5\sin \theta + 6 = 0$ is
- 20. If z is a complex number such that $\frac{z-2}{z+2} = i$, the value of |z| is

 (a) 0 (b) 1 (c) 2 (a) 0(d) 3
- 21. The number of positive divisors of 202300 is
 - (a) 8
- (b) 18
- (c) 26
- (d) 54
- 22. For what values of a and b is the following function continuous at x = 2?

$$f(x) = \begin{cases} ax^2 + bx + 1 & \text{if } x \ge 2\\ 3 & \text{if } x = 2\\ bx^2 - ax - 11 & \text{if } x < 2 \end{cases}$$

- (a) a=1, b=9 (b) a=2, b=12 (c) a=-1, b=3 (d) a=-3, b=-3
- 23. The value of the integral $\int_{0}^{\pi} |\cos 2x| dx$ is

- (c) 2
- (d) 3

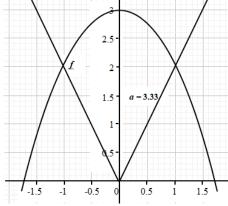






(c)
$$\frac{10}{3}$$





25. Two unbiased dice are thrown simultaneously. What is the probability that both the dice show prime numbers?

(a)
$$\frac{7}{36}$$

(b)
$$\frac{1}{12}$$
 (c) $\frac{1}{6}$

(c)
$$\frac{1}{6}$$

(d)
$$\frac{1}{4}$$

26. The differential equation
$$\frac{dy}{dx} = \frac{y}{x}$$
 represents

- (a) a family of concurrent straight lines
- (b) a family of straight lines passing through (1, 1)
- (c) a family of straight lines parallel to X axis
- (d) a family of straight lines parallel to Y axis
- 27. The volume of a magical right circular cylinder of fixed height changes at a constant rate. Initially, the base radius was 3 units and it changed to 6 units in 3 seconds. What is the radius of the base at time t?

(a)
$$3\sqrt{\pi t + 1}$$

(b)
$$3\sqrt{t+1}$$

(c)
$$3\sqrt{t+\pi}$$

(d)
$$3\sqrt{\pi t + \pi}$$

 $\frac{1}{x^2}\frac{d}{dx}\left(x^2\frac{dy}{dx}\right) + y^n = 0$, is the governing equation for a crude model 28. The Lane Emden equation for a star. Here the star is treated as a sphere of gas with a polytropic equation of state. The differential equation admits exact solutions for polytropic index n = 0, 1 and 5 as $y(x) = 1 - \frac{x^2}{6}$, $\frac{\sin x}{x}$ and $\frac{1}{\sqrt{1+\frac{x^2}{x^2}}}$. The value of $x=x_0$ is such that $y(x_0)=0$ defines the surface of the star.

The quantity $R = \frac{x_0^3}{3\left|-x^2\frac{\mathrm{d}y}{\mathrm{d}x}\right|_{x_0}}$ gives $\frac{\rho_{central}}{\rho_{average}}$ the ratio of the central density to the average density

for the model star. $\left|-x^2\frac{\mathrm{d}y}{\mathrm{d}x}\right|_{x_0}$ means the value of $-x^2\frac{\mathrm{d}y}{\mathrm{d}x}$ evaluated at x_0 . The value of R for n = 0, 1 are

(a) 1,
$$\frac{\pi}{3}$$

(b)
$$\sqrt{6}$$
, $\frac{7}{3}$

(c)
$$\propto$$
, $\frac{\pi^2}{3}$

(b)
$$\sqrt{6}$$
, $\frac{\pi}{3}$ (c) \propto , $\frac{\pi^2}{3}$ (d) 1, $\frac{\pi^2}{3}$

29. The logistic map iteratively maps x_{n+1} to x_n $(n = 0, 1, 2, \dots, m)$ through the equation $x_{n+1} = \lambda x_n (1 - x_n)$. Consider the two different initial values: $x_0 = 0.25$ and $x_0' = x_0 + 0.01 = 0.26$. For $\lambda = 3.25$, the difference between the second iterates $(x_2' - x_2)$ is approximately

(a)
$$0.01$$

$$(b) - 0.01$$

30. In a class of 40 students 25 have opted Hindi as second language (event A). 35 students got first class (event B) in the examinations of which 20 had taken Hindi as second language. It is found that a student picked at random has secured first class. The probability P(A/B) that this student has taken Hindi as second language is

(a) $\frac{4}{7}$

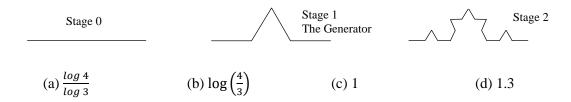
(b) $\frac{5}{9}$

(c) $\frac{7}{9}$

(d) $\frac{1}{2}$

31. When a line segment/square/cube of side length L is measured using a line segment/square/cube of side length l, the number N of line segments/squares/cubes covering the original line segment/square/cube is given by $\left(\frac{L}{l}\right)$, $\left(\frac{L}{l}\right)^2$, $\left(\frac{L}{l}\right)^3$ respectively. Define the dimension of an object as

 $D = [-\log(N)/\log(l)]$ as $l \to 0$. The n = 0, n = 1 and n = 2 steps of iteration of the process of obtaining the fractal curve called a Koch curve, of stretching and bending the middle one third of a line segment (of length L) into a triangle shape of side length L/3 is shown in the figure; in the second (n = 2) iteration each of the 4 line segments of length L/3 will have their middle one third stretched and bend into triangle shapes of side $l = L/(3 \times 3)$. After n iterations the total number N of line segments of length $l = L/3^n$ making up the figure will be 4^n . The dimension D of the Koch curve, obtained as $n \to \infty$ (i.e. as $l \to 0$) is



32. Consider the two sets $G = \{1, i, -i, -1\}$ and $G' = \{R_{\pi/2}, R_{\pi}, R_{3\pi/2}, R_{2\pi}\}$, where R_{θ} stands for rotation of a square by angle θ in the anticlockwise direction about an axis through its centre and perpendicular to its plane. If product of two elements of G is taken by complex multiplication and the product of two elements of G' are taken as $R_{\theta} R_{\varphi} = R_{\theta+\varphi}$, then, under which of the following mappings between G and G' do the product relations hold unchanged?

(a) $\begin{pmatrix} g_1 \to g_1' \\ g_2 \to g_2' \\ g_3 \to g_3' \end{pmatrix}$

(b) $\begin{pmatrix} g_1 \to g_4' \\ g_2 \to g_1' \\ g_3 \to g_3' \end{pmatrix}$ (c) $\begin{pmatrix} g_1 \to g_3' \\ g_2 \to g_4' \\ g_3 \to g_1' \end{pmatrix}$ (d) $\begin{pmatrix} g_1 \to g_2' \\ g_2 \to g_3' \\ g_3 \to g_4' \end{pmatrix}$

33. The objective of a reflecting telescope is a concave mirror of focal length 750 mm. To double the magnification, a concave lens of focal length 20 mm is placed near the focus of the primary mirror. What should be the position of the eyepiece focus from the concave lens?

(a) 10 mm away from mirror

(b) 10 mm towards mirror

(c) 20 mm away from mirror

(d) 20 mm towards mirror

34. On the basis of Bohr Theory of atomic structure, the total energy required to remove both electrons from the helium atom in its ground state is 79 eV. How much energy is required to ionize helium i,e to remove the first electron?

(a) 79.0 eV

(b) 54.4 eV

(c) 39.5 eV

(d) 24.6 eV

35. Five positive charges, each of magnitude q, are arranged symmetrically on the circumference of a circle of radius r. The magnitude of the electric field E at the center of the circle is

(a) Zero

(b) $\frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$ (c) $\frac{1}{\pi\epsilon_0} \frac{q}{r^2}$ (d) $\frac{5}{4\pi\epsilon_0} \frac{q}{r^2}$

36. A particle is constrained to move along a circle of radius R = 1.0 m. At a certain instant of time, the speed of the particle is 1.0 m/s and the speed is increasing at the rate of 1.0 m/s². The angle (in radian) between the velocity and the acceleration vectors of the particle is

(a) Zero

(b) $\frac{\pi}{6}$ (c) $\frac{\pi}{4}$

(d) $\frac{\pi}{2}$

37. A certain amount of helium gas is expanded adiabatically to one and half times of its initial volume. If the initial temperature is 27°C, the final temperature of the gas will be

(a) +3.6°C

(b) -5.8° C

(c) - 10.9°C

(d) - 44.1°C

38. Absorbing a neutron, $\frac{235}{92}U$ undergoes fission producing two fragments in the intermediate atomic mass range namely $^{89}_{36}Kr$ and $^{144}_{56}Ba$ along with three neutrons and energy. By what factor is the size of the so produced $^{144}_{56} Ba$ nucleus smaller than that of the $^{235}_{92} U$ nucleus?

(a) 0.61

39. A small wooden block of mass 2 kg is dropped from a height h = 40 cm on a vertical spring of force constant k = 1960 N/m. The maximum compression of the spring is

(a) 0.1 cm

(b) 1.0 cm

(c) 10.0 cm

(d) 23.0 cm

40. The intensity level of a particular sound source is increased by 10 dB, the corresponding change in the amplitude of the sound wave is

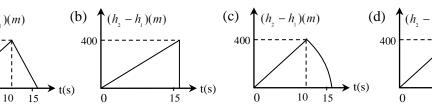
(a) $\sqrt{10}$ times

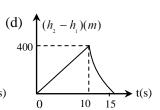
(b) $10\sqrt{10}$ times

(c) 10 times

(d) 100 times

41. Two stones of equal mass are thrown vertically up simultaneously from the edge of a cliff 400 m high with initial speeds of $v_1 = 10 \text{ ms}^{-1}$ and $v_2 = 50 \text{ ms}^{-1}$ respectively. Which of the following graphs best represents the time variation of relative position [height $(h_2 - h_1)$] of the second stone with respect to the first? (Assume that the stones are not obstructed at the cliff while going down and do not rebound after hitting the ground. Also ignore the small horizontal separation between the stones as well as air resistance, take $g = 10 \text{ ms}^{-2}$)





- 42. A crow is sitting on a standard electric power line. The crow is not affected by the potential drop across its feet because
 - (a) it has non-conducting pads at the bottom of its feet
 - (b) the potential drop is too small for any significant current to flow through its body
 - (c) the crow is carefully sitting on the neutral line
 - (d) none of the above

43. Standing waves have been produced in a 51 cm long, open end organ pipe with just one node within the pipe. The wavelength of the sound wave, which forms a standing wave in the same organ

pipe such that there are three nodes within the pipe, is

	(a) 68 cm	(b) 51 cm	(c) 34 cm	(d) 20.4 cm			
44.	44. For the air-glass interface if the Brewster angle (polarizing angle) is ϕ_P , then the critical angle (i _c) for the glass-air interface is expressed as						
	(a) $\sin^{-1}(\tan\phi_P)$		(b) $\cos^{-1}(\tan \phi_p)$.)			
	(c) $\sin^{-1}(\cot \phi_p)$		(d) $\cos^{-1}(\cot\phi_F)$.)			
45.	45. A gas in equilibrium attains a state of equipartition, wherein every active degree of freedom of every particle has on the average the same energy. In particular, the average translational kinetic						
	energy will be the same for every particle; it will be equal to $\frac{3}{2}kT$ where, k is the Boltzmann						
	constant and T is the temperature of the gas in kelvin. Consider air at 300 kelvin. If the root mean square velocity of nitrogen molecules is v_{rms} m/s, the magnitude of the mean velocity and the root mean square velocity of oxygen molecules are respectively						
	(a) $(0, \frac{v_{rms}}{2\sqrt{3}})$		(b) $(0, 0.94v_{rms})$	5)			
	(c) $(\frac{3}{2}v_{rms}, 1.07 v_{rms})$)	(d) (0, $0.875 v_{rr}$	$_{ms})$			
46.	46. Formation of the iron peak elements ${}^{56}_{26}Fe$, ${}^{56}_{27}Co$ and ${}^{56}_{28}Ni$ by nuclear fusion marks the end of energy production in a star. If the mass of the iron core is greater than the Chandrasekhar mass (1.4 solar masses) the core cannot be supported by the degeneracy pressure of the electrons and will collapse to form a neutron star. Matter is crushed to nuclear densities with protons combining with electrons as $p^+ + e^- \rightarrow n + \nu_e$. Neutron stars whose masses are not too high are supported by neutron degeneracy pressure against gravitational collapse. The number of neutrinos released, when a neutron star of 1.4 solar masses forms, is approximately (a) 7.77×10^{56} (b) 1.74×10^{57} (c) 8.68×10^{56} (d) 8.38×10^{57}						
47.	The Seebeck coefficient of gradient is set up across i	a material character	rizes the voltage built the relation $S = -\frac{V_{le}}{V_{le}}$	up when a small temperature $\frac{ft^{-}V_{right}}{}$. Only the relative			
	gradient is set up across it. It is defined by the relation $S = -\frac{V_{left} - V_{right}}{T_{left} - T_{right}}$. Only the relative Seebeck coefficients of materials may be determined since, connecting a voltmeter introduces other voltages. The relative Seebeck coefficients of some elemental materials in $\mu V/K$ are: (A) Aluminium: 3.5 (B) Carbon: 3 (C) Sodium: -2 (D) Platinum: 0. The absolute Seebeck coefficient of Platinum is $-5 \mu V$ at room temperature. The combination of two metals which will give maximum voltage difference when used to make a thermocouple is (a) (A, D) (b) (C, D) (c) (A, C) (d) (B, C)						
48.		owatt per square met	er (kW/m ²). For receive	re from the Sun known as the ring this much power per unit face temperature of (d) 5479 K			

ANY NUMBER OF OPTIONS $(4,3,2\ or\ 1)$ MAY BE CORRECT MARKS WILL BE AWARDED ONLY IF ALL THE CORRECT OPTIONS ARE BUBBLED AND NO INCORRECT

- 49. Consider the electromagnetic radiation emitted by two stars. The hotter star will
 - (a) emit more radiation at all wavelengths
 - (b) have a higher frequency of peak emission in its spectrum
 - (c) radiate energy at more than one wavelength
 - (d) exhibit a continuous spectrum
- 50. Because of the precession of the axis of rotation of Earth
 - (a) the polaris is not always our 'pole star'
 - (b) the average length of a sidereal day changes slowly with time
 - (c) the declinations of the stars change slowly with time
 - (d) the Vernal Equinox moves with respect to the stars
- 51. A planet orbits the Sun at a distance of 4.0 AU from the Sun. The orbital speed (v_o) and the time period (T) of the planet are approximately
 - (a) $v_0 = 7.92 \text{ km/s}$
- (b) $v_0 = 14.93 \text{ km/s}$ (c) T = 4 years
- (d) T = 8 years
- 52. The rotation period of a spherical moon about its own axis is equal to its period of revolution round its parent planet. Which of the following statements is/are true?
 - (a) If the orbital and spin angular momentum vectors of the moon are parallel to each other then, the moon will always show the same portion of its surface to the planet
 - (b) If the spin angular momentum vector of the moon lies in its orbital plane, then every portion of the surface of the moon may be seen from the planet
 - (c) If the orbital and spin angular momentum vectors of the moon are antiparallel with respect to each other then, viewed from the planet, the moon will appear to be non-rotating
 - (d) If the spin angular momentum vector of the moon lies in its orbital plane, then, viewed from the planet, the moon will appear to be rotating with a higher angular speed
- 53. The true statement(s) for the function $f(x) = \begin{cases} \frac{\sin|x|}{|x|} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$ (a) $\lim_{x \to 0} f(x)$ exists

 (b) $\lim_{x \to 0} f(x)$ does not exist

 (c) f is differentiable at x = 0(d) f has removable discontinuation.

- 54. Consider the differential equation $x \frac{dy}{dx} + 3y = x^3$. Which of the following is/are true?
 - (a) $3x^3$ is an integrating factor of this equation
 - (b) $y = \frac{x^3}{6} + \frac{2023}{x^3}$ is a solution of this equation
 - (c) $y = \frac{x^3}{6} \frac{8}{2023 x^3}$ is a solution of this equation
 - (d) The equation is a homogeneous differential equation

- 55. Consider the LPP (Linear Programming Problem) Max Z = x + y subject to the constraints $x+3y \ge 6$, $y \le 3$, $x+y \le 4$, x, $y \ge 0$ Which of the following is/are true?
 - (a) x = 1, y = 2 is a feasible solution of the LPP
 - (b) x = 2, y = 2 is an optimal solution of the LPP
 - (c) The only optimal solutions of the LPP are x=1, y=3 and x=3, y=1
 - (d) x = 3, y = 1 is an optimal solution of the LPP
- 56. For vectors A, B & C in three dimensional Euclidean space, let $AB = A \times B$ stand for the cross product, [A, B] = AB BA for the commutator of A & B and $\{A, B, C\} = (AB) C A$ (BC) for the associator of A, B & C. Then which of the following relations hold true?
 - (a) $A^2 = 0$ for $A \neq 0$
 - (b) [A, B] = 0 for $A \neq B$ and $A, B \neq 0$
 - (c) $\{A, B, C\} = 0 \text{ for } A \neq B \neq C \text{ and } A, B, C \neq 0$
 - (d) A(BC) + B(CA) + C(AB) = 0 for $A \neq B \neq C$ and $A, B, C \neq 0$
- 57. An artificial satellite is moving in an orbit around the Earth with orbital period of 8 hours, from west to east, with its orbit making an angle of 30° with equator. An observer on the equator will see it
 - (a) again after 6 hour, moving from east to west
 - (b) again after about 11 hours, moving from west to east
 - (c) going up to about 46.8° from the equatorial plane
 - (d) going up to about 43.2° from the equatorial plane
- 58. A particle of mass 'm' is moving under the influence of a central force; the correct statement(s) is/are
 - (a) The motion always remains constrained to be in a plane
 - (b) The trajectory will always be elliptical
 - (c) The total angular momentum remains constant
 - (d) The torque about the force center is always zero
- 59. When a raw poori round (kneaded wheat dough rolled into thin rounds) is slipped into hot oil and the hot oil is swished immediately over it repeatedly, the poori puffs up because
 - (a) the dough has comparatively low heat conductivity
 - (b) hot oil causes a crust to form
 - (c) the density of steam is low
 - (d) the matrix of proteins in the dough formed during kneading helps trap gases
- 60. Two positively charged conducting spheres A and B with +Q charge on each, are placed on the x-axis at (a, 0) and (-a, 0). A very small metallic ball with charge +q is gently placed at the origin (midway between the two spheres). The small ball with charge +q, in the middle, is
 - (a) in stable equilibrium if constrained to move only along x-axis
 - (b) in unstable equilibrium if constrained to move only perpendicular to the x-axis
 - (c) always in unstable equilibrium
 - (d) always in neutral equilibrium

Rough Work