

#### **SAMPLE PAPER**

# 10

#### **CREST Mathematics Olympiad (CMO)**

#### Syllabus for CMO is available at <a href="https://www.crestolympiads.com/cmo-syllabus">https://www.crestolympiads.com/cmo-syllabus</a>

Pattern And Marking Scheme				
Class	Topic/Section	No. of Questions	Marks per Questions	Total Marks
	Practical Mathematics	25	1	25
1 <sup>st</sup> to 4 <sup>th</sup>	Achiever's Section	10	2	20
	<b>Grand Total</b>	35	-	45
	Practical Mathematics	40	1	40
5 <sup>th</sup> to 10 <sup>th</sup>	Achiever's Section	10	2	20
	<b>Grand Total</b>	50	-	60

1. If  $\sqrt{a} > \sqrt{b} > \sqrt{c} > \sqrt{d}$ , where a, b, c and d are consecutive natural numbers, then which of the following is true?

(a) 
$$\sqrt{a} - \sqrt{b} > \sqrt{c} - \sqrt{d}$$

(b) 
$$\sqrt{c} - \sqrt{d} > \sqrt{a} - \sqrt{b}$$

(c) 
$$\sqrt{c} - \sqrt{d} = \sqrt{a} - \sqrt{b}$$

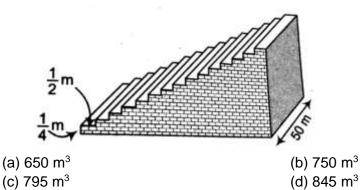
- 2. Places A and B are 100 km apart on a highway. One car starts from A and another from B at the same time. If the car travels in the same direction, then they meet in 5 hours. If they travel towards each other, then they meet in 1 hour. Find the speeds of both the cars:
  - (a) 60 km/h, 40 km/h

(b) 30 km/h, 45 km/h

(c) 45 km/h, 60 km/h

(d) 75 km/h, 90 km/h

3. A small terrace at a football ground comprises of 15 steps, each of which is 50 m long and built of solid concrete. Each step has a rise of 1/4 m and a tread of 1/2 m. Calculate the total volume of concrete required to build the terrace:



- 4. The co-ordinates of the mid-points of the sides of a triangle are (4, 2), (3, 3) and (2, 2). What will be the co-ordinates of the centroid of the triangle?
  - (a) (3, 7/3)

(b) (-3, -7/3)

(c) (3, -7/3)

- (d) (-3, 7/3)
- 5. The decorative block shown in the figure given below is made of two solids, a cube and a hemisphere. The base of the block is a cube with the edge 5 cm and the hemisphere fixed on the top has a diameter of 4.2 cm. Find the total surface area of the block:



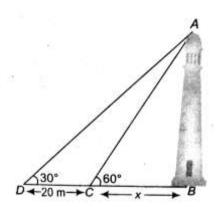
- (a) 150 cm<sup>2</sup>
- (c) 162.86 cm<sup>2</sup>

- (b) 160.86 cm<sup>2</sup>
- (d) 163.86 cm<sup>2</sup>

- 6. There are 35 cards numbered from 1 to 35. A card is selected at random. What is the probability that the drawing card will be a:
  - (i) multiple of 3 or 5.
  - (ii) prime number
  - (iii) multiple of 7, respectively?
  - (a) 15/35, 9/35, 1/5

(c) 16/35, 11/35, 1/7

- (b) 19/35, 12/35, 12/35
- (d) 21/35, 10/35, 9/35
- 7. A TV tower stands vertically on a bank of a canal. From the point on the other bank, directly opposite the tower, the angle of elevation of the top of the tower is 60°. From another point 20 m away from this point on line joining this point to the foot of the tower, the angle of elevation of the top of the tower is 30°. Find the height of the tower:



- (a) 10√3 m
- (c) 15 m

- (b) 10 m
- (d) 24 m

8. An archery target has three regions formed by three concentric circles as shown in the figure given below. If the diameters of the circles are in the ratio 1: 2: 3, then find the ratio of the areas of three regions:



(a) 1: 2: 4

(c) 1: 3: 5

(b) 1: 3: 4

(d) 2: 3: 4

### **Achiever's Section**

9. Let ABC be a right-angled triangle in which AB = 3 cm, BC = 4 cm and angle B = 90°. BD is the perpendicular from B on AC. The circle through B, C and D is drawn. The steps of constructions of a pair of tangents from A to this circle is given below. Which of the following steps is incorrect?

Step I: Draw triangle ABC and perpendicular BD from B on AC.

Step II: Draw a circle with BC as a diameter. This circle will pass through D.

Step III: Let O be the mid-point of BC. Join AO.

Step IV: draw a circle with AO as diameter. This circle cuts the circle drawn in step II at B and P. Join AO, AP and AB are desired tangents drawn from A to the circle passing through B, C and D.

(a) Only step I

(b) Only step II

(c) Only step III

(d) Only step IV

- **10.** If the four sides of a quadrilateral ABCD are tangential to a circle, then which of the following is true?
  - (a) AC + AD = BD + CD
  - (b) AB + CD = BC + AD
  - (c) AB + CD = AC + BD
  - (d) AC + AD = BC + AB

#### **Answers**

1. (b), 2. (a), 3. (b), 4. (a), 5. (d), 6. (c), 7. (a), 8. (c), 9. (d), 10. (b)