## BLOOM PUBLIC SCHOOL

C-8 Vasant Kunj, New Delhi

Mid- Term Examination Sample Paper (2022-23)

## Mathematics (041)

Class - X

## Date:

Time Allowed: 3 hours
Max. Marks: 80

## General Instructions:

- All questions are compulsory.
- This question paper consists of 38 questions divided into 5 sections A, B, C, D and E.
- Section A comprises of 20 questions of one mark each (from Q1-20).
- Section B comprises of 5 questions of two marks each (from Q21-25).
- Section C comprises of 6 questions of three marks each (from Q26-31).
- Section D comprises of 4 questions of five marks each (from Q32-35).
- Section E comprises of 03 case study questions of 4 marks each (from Q36-38).
- There is no overall choice. However, internal choice has been provided in 02 questions of section $B, 02$ questions of section $C, 02$ questions of section $D$ You have to attempt only one of the alternatives in such questions.

|  | Section A | 20 M |
| :---: | :---: | :---: |
| Q1 | Assertion : The HCF of two numbers is 5 and their product is 150 , then their LCM is 30 <br> Reason : For any two positive integers a and $\mathrm{b}, \operatorname{HCF}(\mathrm{a}, \mathrm{b})+$ $\operatorname{LCM}(\mathrm{a}, \mathrm{b})=\mathrm{a} \times \mathrm{b}$ <br> (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A). <br> (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A). <br> (c) Assertion (A) is true but reason (R) is false. <br> (d) Assertion (A) is false but reason (R) is true. | 1 |
| Q2 | What is the value of k such that the following pair of equations have infinitely many solutions? $x-2 y=3 \text { and }-3 x+k y=-9$ <br> a) 6 <br> b) 3 <br> c) -3 <br> d) -6 | 1 |
| Q3 | For what value of $p$ does the pair of linear equations given below has unique solution? $4 x+p y+8=0 \quad 2 x+2 y+2=0$ <br> (a) $p=1$ (b) $p=2$ (c) $p \neq 4$ <br> (d) $p \neq 2$ | 1 |
| Q4 | The roots of the equation $x^{2}+7 x+10=0$ are <br> a) $-5,-2$ <br> b) 5,2 <br> c) $5,-2$ <br> d) $-5,2$ | 1 |
| Q5 | Values of k for which the quadratic equation $2 \mathrm{x}^{2}-\mathrm{kx}+\mathrm{k}=0$ has equal roots is | 1 |


|  | a) $0 \begin{array}{llll}\text { b) } 4,0 & \text { c) } 8 & \text { d) } 0,8\end{array}$ |  |
| :---: | :---: | :---: |
| Q6 | The nth term of an AP a $, 3 \mathrm{a}, 5 \mathrm{a}, \ldots \ldots$ is <br> a) na <br> b) $(2 n-1) \mathrm{a}$ <br> c) $(2 n+1) a$ <br> d) 2 na | 1 |
| Q7 | For what value of k will $\mathrm{k}+9,2 \mathrm{k}-1$, and $2 \mathrm{k}+7$ are the consecutive terms of an AP? <br> a) 16 <br> b) 2 <br> c) 18 <br> d) 4 | 1 |
| Q8 | Which of the following statement(s) is/ are false? <br> (i) All isosceles triangles are similar. <br> (ii) All quadrilaterals are similar. <br> (iii) All circles are similar. <br> (iv) All squares are similar <br> a) i) and iii) <br> b) i) and ii) <br> c) iii) and iv) d) ii) and iv) | 1 |
| Q9 | Assertion : The value of $\sin \mathrm{A}=\frac{4}{3}$ is not possible. <br> Reason: Hypotenuse is the largest side in any right angled triangle. <br> (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A). <br> (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A). <br> (c) Assertion (A) is true but reason (R) is false. <br> (d) Assertion (A) is false but reason (R) is true. | 1 |
| Q10 | The line represented by $4 \mathrm{x}-3 \mathrm{y}=9$ intersects the y axis at <br> i) <br> $(0,-3)$ <br> ii) $\left(\frac{9}{4}, 0\right)$ <br> iii) $(-3,0)$ <br> iv) $\left(0, \frac{9}{4}\right)$ | 1 |
| Q11 | Find the sum of the exponents of the prime factors in the prime factorisation of 196. | 1 |
| Q12 | The LCM of two numbers is 182 and their HCF is 13. If one of the numbers is 26 , find the other. | 1 |
| Q13 | Write the discriminant of the quadratic equation $(x+5)^{2}=2(5 x-$ 3). | 1 |
| Q14 | The pair of equations $\mathrm{y}=0$ and $\mathrm{y}=-7$ has ___ solution(s). | 1 |
| Q15 | Which term of the following AP $27,24,21 \ldots \ldots$ is 0 . | 1 |
| Q16 | How many two digit numbers are divisible by 3 ? | 1 |
| Q17 | Write the coordinates of the centre of the circle whose end points of a diameter are $(-6,3)$ and $(6,4)$. | 1 |
| Q18 | In the given figure, $\mathrm{DE} \\| \mathrm{BC}$. The value of EC is | 1 |
| Q19 | If $\sin \mathrm{A}+\cos \mathrm{B}=1, \mathrm{~A}=30^{\circ}$ and B is an acute angle. Find the value of $B$. | 1 |
| Q20 | If $\triangle A B C$ is right angled at $C$, then the value of $\cos (A+B)$ is | 1 |


|  | Section B |  |
| :---: | :---: | :---: |
| Q21 | Find the smallest number that is a perfect square and is divisible by $16,20,24$. | 2 |
| Q22 | Find the quadratic polynomial whose zeroes are $(5-3 \sqrt{ } 2)$ and $(5+3 \sqrt{2})$. | 2 |
| Q23 | If the $8^{\text {th }}$ term of an AP is zero. Prove that its $38^{\text {th }}$ term is triple of its $18^{\text {th }}$ term. | 2 |
| Q24 | Find the perimeter of a triangle with vertices $(0,4),(0,0)$ and $(3,0)$. <br> OR <br> Find a linear relation between x and y such that $\mathrm{P}(\mathrm{x}, \mathrm{y})$ is equidistant from the points $\mathrm{A}(1,4)$ and $\mathrm{B}(-1,2)$ | 2 |
| Q25 | The value of $\left(\sin ^{2} \mathrm{~A}+\frac{1}{1+\tan ^{2} A}\right)=$ <br> OR <br> If $\operatorname{cosec} \theta=\frac{3}{2}$, find the value of $2\left(\operatorname{cosec}^{2} \theta+\cot ^{2} \theta\right)$ | 2 |
|  | Section C |  |
| Q26 | Using prime factorisation method, find the HCF and LCM of 72,126 and 168 . Also show that HCF x LCM $\neq$ product of three numbers. | 3 |
| Q27 | If $\alpha$ and $\beta$ are the zeroes of the polynomial $x^{2}-5 x+6$, then find the value of $\frac{1}{\alpha^{2}}+\frac{1}{\beta^{2}}$. <br> OR <br> If $\alpha$ and $\beta$ are the zeroes of the polynomial $2 y^{2}-y-2$, then find the quadratic polynomial whose zeroes are $2 \alpha$ and $2 \beta$. | 3 |
| Q28 | In a flower bed, there are 23 rose plants in the first row, 21 in the second, 19 in the third and so on. There are 5 rose plants in the last row. How many rows are there in all and the total number of rose plants? <br> OR <br> Raj's friend Veer wants to participate in a 200 m race. He can currently run the distance in 51 seconds. With each day's practice it takes him 2 seconds less. He wants to do it in 31 seconds. What is the minimum number of days he has to practice to achieve his goal? | 3 |
| Q29 | In a trapezium, show that any line drawn parallel to the parallel sides of the trapezium divides the non-parallel sides proportionally. | 3 |
| Q30 | Find the coordinates of point R on the line segment joining the points $\mathrm{P}(-1,3)$ and $\mathrm{Q}(2,5)$ such that $\mathrm{PR}=\frac{3}{5} \mathrm{PQ}$. | 3 |
| Q31 | Show that $\sec ^{4} \theta-\operatorname{Sec}^{2} \theta=\tan ^{4} \theta+\tan ^{2} \theta$ | 3 |
|  | Section D |  |
| Q32 | Check graphically whether the pair of linear equations $4 x-y-8=0$ and $2 x-3 y+6=0$ is consistent. Also find the vertices of the triangle formed by these lines with the x -axis. | 5 |


| Q33 | A two-digit number is such that the product of its digits is 24 . If 18 is subtracted from the number, the digits interchange their places. Find the number. <br> OR <br> A and B working together can do a work in 6 days. If $A$ takes 5 days less than B to finish the work, in how many days B alone can do the work? | 5 |
| :---: | :---: | :---: |
| Q34 | If $\sqrt{ } 3 \sin \theta=\cos \theta$, find the value of $\frac{\sin \theta \tan \theta(1+\cot \theta)}{\sin \theta+\cos \theta}$. <br> OR <br> If $\sec \theta-\tan \theta=x$, show that $\sec \theta+\tan \theta=\frac{1}{x}$ and hence find the values of $\cos \theta$ and $\sin \theta$. | 5 |
| Q35 | a) State and prove Thale's Theorem. <br> b) In $\triangle A B C, D E \\| B C$. Find $x$. | 5 |
|  | Section E |  |
| Q36 | A barrels manufacturer can produce up to 300 barrels per day. The profit made from the sale of these barrels can be modelled by the function $P(x)=-10 x^{2}+3500 x-66000$ where $P(x)$ is the profit in rupees and $x$ is the number of barrels made and sold. <br> a) When no barrels are produce what is the profit/loss? <br> i) Rs 22000 <br> ii) Rs 66000 <br> iii) Rs 11000 <br> iv) Rs 33000 <br> b) What is the profit/loss if 175 barrels are produced? <br> i) Profit ₹ 266200 <br> ii) Loss ₹ 266200 <br> iii) Profit ₹ 240250 <br> iv) Loss ₹ 240250 <br> c) What is the number of barrels made and sold to breakeven? (Zero profit point is called breakeven) | $\begin{aligned} & \hline 4 \\ & (1+1+2) \end{aligned}$ |
| Q37 | Ajay, Bhavya and Colin are fast friend since childhood. They always want to sit in a row in the classroom. Bhavya is very | $\begin{array}{\|l\|} \hline 4 \\ (1+1+2) \\ \hline \end{array}$ |


|  | good in maths and he does distance calculation every day. He considers the centre of class as origin and marks their position on a paper in a co-ordinate system. One day Bhavya makes the following diagram of their seating position. <br> a) What is the distance of point A from origin? <br> i) 8 <br> ii) $2 \sqrt{ } 2$ <br> iii) 4 <br> iv) $4 \sqrt{ } 2$ <br> b) What is the distance between $A$ and $B$ ? <br> i) $3 \sqrt{ } 19$ <br> ii) $3 \sqrt{ } 5$ <br> iii) $\sqrt{ } 17$ <br> iv) $2 \sqrt{ } 5$ <br> c) A point D lies on the line segment between points A and $B$ such that $\mathrm{AD}: \mathrm{DB}=4: 3$. What are the coordinates of point D ? |  |
| :---: | :---: | :---: |
| Q38 | Saving a certain amount for future is a good habit. Ramesh is student of class X and he inculcated the habit of saving. Recently, Ramesh have received a Prize Money of Rs 10000 in an Art competition. He deposited it with a bank. The bank offers him a simple interest at the rate of $6.5 \%$ per year. He has a plan to use this money to some books and stationary. <br> a) What is the interest he receives in the first year? i)Rs 650 <br> ii) Rs 65 <br> iii) Rs 6500 <br> iv) Rs 10000 <br> b) What is the total money he receives after 10 years? <br> Rs 6500 ii) Rs 10650 <br> iii) Rs 16500 <br> iv) Rs10000 <br> c) Write the sequence for the amount of money at the end of each year. What kind of sequence is it and why? | $\begin{aligned} & 4 \\ & (1+1+2) \end{aligned}$ |

